

Repeating Decimals

How to write repeating decimals

We draw a line above decimal digits when they repeat over and over again.

For example: $0.\overline{3}$ is the same as 0.33333333333333... (and so on)

$0.\overline{25}$ is the same as 0.25252525252525... (and so on)

$0.12\overline{34}$ is the same as 0.123434343434... (and so on)

1. Use a calculator to change these fractions into decimals. Try to use the notation described above.

$$\frac{2}{3} = \underline{0.\overline{6}}$$

$$\frac{3}{11} = \underline{0.\overline{27}}$$

$$\frac{5}{6} = \underline{0.\overline{83}}$$

$$\frac{50}{99} = \underline{0.\overline{50}}$$

2. Follow along with your teacher to show how to convert a repeating decimal into a fraction.

Let $x = 0.\overline{45}$

$$\begin{array}{r} 100x = 45.\overline{4545} \\ - x = 0.\overline{4545} \\ \hline 99x = 45 \\ \frac{99x}{99} = \frac{45}{99} \\ x = \frac{45}{99} = \frac{5}{11} \end{array}$$

Let $x = 0.\overline{16}$

$$\begin{array}{r} 10x = 1.\overline{6666} \\ - x = 0.\overline{1666} \\ \hline 9x = 1.5 \\ \frac{9x}{9} = \frac{1.5}{9} \\ x = \frac{1.5}{9} = \frac{15}{90} = \frac{1}{6} \end{array}$$

3. Change each of these decimals into fractions. Show all work.

<p>★</p> <p>0.54</p>	<p>$0.\overline{3}$</p>	<p>$0.\overline{54}$</p>
<p>$0.5\overline{4}$</p>	<p>$0.\overline{72}$</p>	<p>$0.41\overline{6}$</p>